

- $m = n$  Same number of rows as columns.
- **Determinant:**  $\det(A) = |A|$
- **Trace:** Sum of diagonal entries.  $\text{tr}(A) = a_{11} + a_{22} + \dots + a_{nn}$
- **Symmetric Matrix:** A square matrix such that  $A = A^T$ 
  - The sum of symmetric matrices is also symmetric.
  - A symmetric matrix multiplied by a scalar is symmetric.
  - An inverse of a symmetric matrix is also symmetric, if it exists.
- **Skew-symmetric Matrix:** A square matrix such that  $A = -A^T$ 
  - The sum of skew-symmetric matrices is also skew-symmetric.
  - A skew-symmetric matrix multiplied by a scalar is skew-symmetric.
  - An inverse of a skew-symmetric matrix is also skew-symmetric, if it exists.
- **Idempotent Matrix:** A square matrix such that  $A^2 = A$ .
  - Determinant is either 0 or 1
- **Nilpotent Matrix:** A square matrix such that  $A^k = O$  for some  $k$ .
  - Zero entries along diagonal.
  - Determinant is 0.
- **Orthogonal Matrix:** A square matrix such that  $A^{-1} = A^T$ .
- **Diagonal Matrix:** All entries off the main diagonal are 0.
- **Triangular Matrix**
  - **Upper triangular:** All entries above the diagonal are 0
  - **Lower triangular:** All entries below the main diagonal is 0.
  - The transpose of upper triangular is lower triangular and vice versa.
  - The product of two upper triangular is upper triangular.
  - The product of two lower triangular is lower triangular.
  - Invertible iff diagonal entries are non-zero.
  - Inverse of upper triangular is upper triangular if it exists.
  - Inverse of lower triangular is lower triangular if it exists.
  - Determinant is the product of diagonal entries.